Required Outcomes from Core Computational Thinking

In building the Computer-Based Maths curriculum, we came to a startling realisation: we couldn’t find an effective listing of outcomes to reflect what the core subject should be. So we set about building it—all 11 dimensions:

**WHOLE PROCESS OUTCOMES:**

**CPr**  
Recalling the four-step process  
Knowing the names and sequence of the four steps.

**CPa**  
Applying the four-step process  
Showing knowledge of the purpose of each step and being able to manage the process through to a solution or conclusion.

**CPm**  
Managing the process of breaking large problems into small problems  
Having the confidence to manage a problem larger than the student thinks they can do or has experience of solving. Being able to recombine all of the smaller problems to form a solution to the large problem.

**CPt**  
Applying existing tools in new contexts  
Being able to use a tool you have learnt in a context different from where it has been learnt. Having the confidence to adapt the tool to a new purpose.

**CPk**  
Knowing how to teach yourself new tools  
Knowing where to find guidance on the use of a new tool. Being able to follow instructions or an algorithm.

**CPi**  
Interpreting others’ work  
Reading reports from other sources. Understanding problem solutions that others have proposed. Having confidence to question source.

**CONFIDENCE TO TACKLE NEW PROBLEMS**

Students show confidence to attempt solutions to new problems by application of the four-step process. They use the problem-solving process as a mechanism to overcome hard-to-handle or unknown scenarios and can adapt previously learned methods, concepts and tools to new contexts. They are able to overcome sticking points in the process and teach themselves new tools as the need arises.
Students are able to use their experience to know when something just “smells” wrong. They are aware of common errors made and have a working mental knowledge of the use of concepts and tools.

*IFu*  
**Identify the usefulness of computational thinking for a given real-world problem**  
When presented with a fuzzy situation, students can identify whether computational thinking effectively applies or not.

*IFp*  
**Assessing the plausibility of computational thinking being useful**  
When presented with a fuzzy situation, students can propose ideas of areas of computation that might apply or be clear that computation cannot effectively help.

*IFF*  
**Identifying fallacies and misuse of computation**  
Identifying flaws in logic or improper application of concepts.

*IFr*  
**Having a feel for how reliable a model will be**  
- Having a gut feel for the model and whether it takes into account all the effects that are fundamental to a useful prediction.  
- Understanding that a given problem’s time frame, the number of variables involved and the breadth of concepts applicable all affect the complexity and difficulty in building an accurate model.  
- Appreciating how uncertainties propagate.

*IFe*  
**Estimating a solution of the defined problem**  
Estimating solutions before beginning the problem-solving process. Anticipating the structure of the solution to expect. Structures include: number of dimensions, periodicity, distribution, topology, piecewise nature, constant/variable, domain and time sensitivity.

### CRITIQUING AND VERIFYING

Critiquing is a consideration of what could possibly be wrong with your process or solution. Asking the questions: Where? When? Why? What? Who? It is a constant process of scepticism towards results, from unexpected results to expected results. Verifying is comparing against a hypothesis to confirm an answer and being able to justify the result.

*CVa*  
**Quantifying the validity and impact of the assumptions made**  
For the assumptions stated in DQ, comparing the relative probability of each being invalid and the impact that this would have on the method or solution.

*CVl*  
**Quantifying the validity and impact of tools and concepts chosen**  
For the tools and concepts chosen, comparing the relative probability of each being invalid and the impact that this would have on the method or solution.
CVc  Listing possible sources of error from computation failures or limitations
Division by zero. Implications of sign changes. Accuracy limitations, etc.

CVm  Listing possible sources of error from concepts’ limitations
For the concepts used, list the circumstances in which they would not apply or the extent to which they begin to fail at extremes.

CVE  Identifying systematic and random errors
Spotting that the actual methods used for a solution are wrong. Identifying reasons for an unexpected output dependent upon certain conditions.

CVt  Being able to corroborate your results
Appeal to different methods. Verify that the final model produces the same output as the combined individual components. Test on an independent dataset.

CVr  Qualifying reliability of sources
Determine the source of data collection, the source of a model to use, the research behind a particular method. Understand the criteria for assessing whether a source is reliable.

CVd  Deciding if the results are sufficient to move to the next step, including whether to abandon
All through the problem-solving cycle, deciding whether the current progress is sufficient to move forwards, repeat the cycle or abandon the process.

GM  GENERALISING A MODEL/THEORY/APPROACH

Once a model has been built for a specific purpose, looking further afield for instances where the model may apply or providing sufficient documentation for others to adapt the model for their purpose.

GMi  Identify similarities and differences between different situations for the purposes of abstraction
Identify similar structures, dimensions, flow or patterns between two problems or contexts.

GMv  Taking constants from initial model and making them variable parameters
Broadening the application of the model/solution by releasing constraints or varying assumptions made.

GMw  Being able to draw wider conclusions about the behaviours of a type of problem
Using experience of a concept or tool to extrapolate or extend its use. Testing what happens at extremes or at key points for the dependent variables.

GMg  Implementing a generalised model as a robust program
Providing details and limits of the assumptions made and the variables involved. Providing documentation for reference and thorough testing of the model.
Communicating and collaborating is a continual process that happens throughout all stages. Students use media fit for the purpose and combine multiple representations effectively for the intended audience to be able to follow the ideas presented.

**CCv**  Distilling or explaining ideas visually
Constructing or using visual explanations of ideas during the problem-solving cycle. Small scale, informal sketches or diagrams that allow progress to be made. These may be in the form of the structure of the problem, connections or relationships between variables, trends (the shape of data), positional references, dimensionality, showing how the problem changes from one state to the next.

**CCp**  Distilling or explaining ideas verbally
Briefly explaining reasons, describing an approach to a solution or interpreting an output they are given. The ability to form a verbal description of the point they are trying to make.

**CCd**  Distilling or explaining ideas through written description
Similar to CCp but communicating through written text. Small, individual pieces, a few lines to explain an idea.

**CCc**  Using vocabulary, symbols, diagrams, code accurately and appropriately for your audience
At the correct level for technical understanding, to communicate an idea, to advance understanding, to communicate your findings.

**CCb**  Choosing the best form of communication for a given purpose
Combining multiple forms of media as necessary to convey the ideas and solutions.

**CCr**  Structuring and producing a presentation or report
Organising a clear account of the problem, how it was solved and its solution. Written at a level suitable for the audience intended.

**CCg**  Being able to work effectively in a group to solve a problem
Understand how to iterate a problem in a group and give opinions when appropriate.

**CCf**  Deciding which facts support or hinder an argument
Being able to identify those facts that support your case and those that do not. Defending opinions and inferences made in real time; debating.

**CCI**  Understanding and critiquing ideas presented to you
Being able to identify flaws or gaps in an explanation. Being able to ask effective questions to improve your understanding.

**CCq**  Using techniques for questioning, interrogation, cross-examining
Being able to draw out the information that you want.
INDIVIDUAL STEP OUTCOMES:

DEFINING THE QUESTION

Students begin the problem-solving process by organising the information needed to solve the problem and identifying suitable smaller tasks that can be solved. They understand assumptions and use them effectively to aid progress on the solution.

DEFINE QUESTIONS: STEP 1 OF THE COMPUTATIONAL THINKING PROCESS

**DQ**

- **DQf** Filtering the relevant information from available information
  - Identifying dependencies related to the problem.

- **DQm** Identifying missing information to be found or calculated
  - Identifying dependencies related to the problem about which there is no information.

- **DQq** Stating precise questions to tackle
  - Efficiently presenting the problem to be solved, with an accurate definition of the scope and nature of the problem and variables involved.

- **DQa** Identifying, stating and explaining assumptions being made
  - Clearly states assumptions that have been made and the reasons why. Assumptions are made to avoid complexity in the problem setup or to avoid irrelevant solutions. Care should be taken that assumptions are not made to avoid computational complexity as is often done without a computer. Consideration of the likelihood of an assumption is sometimes necessary as the list of all possible assumptions could be very long.

ABSTRACTING TO COMPUTABLE FORM

Students begin the abstraction phase by taking their precise questions and working out strategies or concepts to explore. They organise their information and identify the relevant concepts and their suitability for the purpose.

ABSTRACT TO COMPUTABLE FORM: STEP 2 OF THE COMPUTATIONAL THINKING PROCESS

**AC**

- **ACp** Identifying the purpose of the abstraction
  - Reduce the amount of information, create linkages, state the reason for it.

- **ACd** Creating diagrams to structure knowledge
  - Organising the information related to a given problem to make applicable concepts easier to identify. Making connections between concepts or data, organising the flow or dependencies of variables involved in the problem. Links to CCv.
ACc  Identifying relevant concepts and their relationship
Listing concepts and filtering down to those which may apply. Making connections amongst the concepts.

ACr  Understanding the relative merits of the concepts available
Comparing the choice of concepts for this abstraction.

ACa  Being able to present alternative abstractions
Diagrams, symbolic representations (programs, expressions), structure information (tables, lists, matrices).

CONCEPTS

Concepts are what you want to get done (hang a picture, solve an equation, describe an event’s probability...). Tools are what you want to use to do it (glue, nail, screw, graph, formula, normal distribution...). Most concepts begin life with one tool; you invent the concept for a given problem and a tool to fix that. Though retrospectively, people might collect a number of tools and create an umbrella concept to cover them.

ABSTRACT TO COMPUTABLE FORM: STEP 2 OF THE COMPUTATIONAL THINKING PROCESS

C1  Being able to describe the concept
Describing the structure of the concept and giving examples of its application, purpose and limitations.

C2  Recognising whether the concept applies
For the chosen concept in the context of the problem.

C3  Knowing which tools are relevant to the concept
For the chosen concept in the context of the problem, including where there are no tools available for particular cases: the solution of a quintic equation, for example.

C4  Having intuition for the relative merits of the concept
For the chosen concept in the context of the problem compared to other possible concepts that may be of use in this context.
Tools take the form of functions, methods or processes that enable a conversion from the abstracted form of the defined question into a form that is useful in answering the question. The tool may not necessarily be computer based. The most efficient manifestation of the tool for the purpose should be chosen.

**ABSTRACT TO COMPUTABLE FORM: STEP 2 OF THE COMPUTATIONAL THINKING PROCESS**

- **Tb** Having intuition about the tool's behaviour
  Knowing how the tool behaves in a wide variety of contexts. Understanding its strengths, weaknesses and competitive advantage under certain circumstances.

- **Ti** Composing appropriate and accurate input for the tool
  Organising data into the correct format, changing units, limiting domains, setting accuracies, ordering, filtering, setting the options required.

- **Ta** Applying the tool or demonstrating experience of its application
  Knowing how to run or evaluate the tool to produce a result.

- **Tc** Being aware of comparable tools
  Related tools to this tool only. Tools that achieve similar aims without being a direct replacement.

- **Tr** Understanding the relative merits of different tools for use in the context
  Related tools to this tool only. There is a possible feedback loop: if your tools are not good enough for the job, you may need to jump concept.

**MANAGING COMPUTATIONS**

The computation phase begins with students choosing the manifestation of the tool(s) to produce a result. This may be a trivial step for one tool with a simple input but could also be organisationally complex for combinations of a number of tools. Once the computation reaches a certain size, the process of performing the computation becomes a significant consideration.

**COMPUTE ANSWERS: STEP 3 OF THE COMPUTATIONAL THINKING PROCESS**

- **MC1** Choosing an appropriate technology
  Choosing between various forms of technology (hardware/software), physical machine or brain power.
MC2  Being able to interpret documentation
  • Accessing documentation and using it to inform the use of the tool in the context that is
    required.
  • For code, documentation is the formal information supplied for the use of a defined function.
    For other types of tools, this also includes video descriptions, informal notes, help systems or
    websites.

MC3  Assessing the feasibility of getting a useful answer
  • A preflight checklist before take-off. A “yes, ok” or “no go” check on the computation.
  • Questioning if the errors involved are going to overwhelm the result and a useful solution will
    not be achieved.
  • Questioning whether it is feasible to find the solution within a reasonable time.

MC4  Having intuition about whether the output is appropriate for the context
  • Not interpreting, just an instinctive feel if the output is off.
  • Checking variable types, dimensions and magnitudes instinctively.

MC5  Combining tools to produce results required
Constructing a computation using a combination of tools or processes to produce a solution.
Linking tools together, ensuring that an output of one tool is suitable as the input of another.

MC6  Isolating the cause(s) of operational problems
Knowing systematic methods for identifying the issue. Knowing how to remove parts of the
process to isolate suspect parts. Checking units, checking logic, checking structure, checking
size, etc.

MC7  Resolving operational problems
Knowing what to do if the computer takes too long to calculate or cannot handle the size or
accuracy needed for the computation.

MC8  Optimising both speed of obtaining results and reusability of computation
Deciding between a back-of-the-envelope quick calculation versus full reporting and delivering
communicable methods. Weighing up the usefulness of spending time on documentation versus
time on progression to a solution.
## INTERPRETING

Students take the output of the computation stage and translate this back to the original real-world problem by relating the output to their precise question. They consider further areas of investigation as a result.

**INTERPRET RESULTS: STEP 4 OF THE COMPUTATIONAL THINKING PROCESS**

1. **IN1  Reading common and relevant representations and notations**  
   Being able to read out visualisations, notations, values and units being shown without interpretation. Commonly used notations or those which are specific to a primary context.

2. **IN2  Making statements about the output in the context of the original problem**  
   Specific values of the output in terms of the original question. Consideration of the units of the required solution. Statements to show understanding of the reading of the information.

3. **IN3  Identifying and relating features of the output to real-world meaning**  
   General features of the output like the shape, maxima, minima, steepest slope, asymptotes, dimensions, units, etc.

4. **IN4  Identifying interesting features in results**  
   Very specific interesting features from those identified in IN3 that are relevant to the original problem.

5. **IN5  Inferring a hypothesis beyond the current investigation**  
   Giving a subjective slant. Reasoning why. Hypothesising or drawing to a conclusion. Extrapolating. Interpolating. Links to GM.